



**Unit 4**

**Syllabus**

**Digital Electronics:** Number system & representation, Binary arithmetic, Introduction of Basic and Universal Gates, using Boolean algebra simplification of Boolean function. K Map Minimization upto 6 Variables.



## Number System

There are many different symbols are used in no.

- ① Binary  $\rightarrow$  Base 2 (0, 1)
- ② Octal  $\rightarrow$  Base 8 (0, 1, 2, 3, 4, 5, 6, 7)
- ③ Decimal  $\rightarrow$  Base 10 (0, 1, 2, 3, 4, 5, 6, 7, 8, 9)
- ④ Hexadecimal  $\rightarrow$  Base 16 (0, 1, 2, 3, 4, 5, 6, 7, 8, 9, A, B, C, D, E, F)

## Conversion

$\rightarrow$  Any no to decimal number system

Ex  $[101.010]_2$  to decimal

$$\begin{array}{r}
 1 \times 2^2 \\
 0 \times 2^1 \\
 1 \times 2^0
 \end{array}
 \left[ \begin{array}{c}
 2 \\
 1 \\
 0 \\
 -1 \\
 -2 \\
 -3
 \end{array} \right]
 \begin{array}{r}
 0 \times 2^{-1} \\
 1 \times 2^{-2} \\
 0 \times 2^{-3}
 \end{array}$$

$$4 + 0 + 1 + 0 + 2^{-2} + 0$$

$$5 + \frac{1}{4} = (5.25)_{10}$$

$$\textcircled{1} [4021.3]_5$$

$$\begin{array}{r}
 4 \times 5^3 \\
 0 \times 5^2 \\
 2 \times 5^1 \\
 1 \times 5^0
 \end{array}
 \left[ \begin{array}{c}
 3 \\
 2 \\
 1 \\
 0 \\
 -1
 \end{array} \right]
 \begin{array}{r}
 3 \times 5^{-1}
 \end{array}$$

$$= 500 + 10 + 1 + 0.4$$

$$= [511.4]_{10}$$



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## Unit 1

### Number System

There are many different symbols are used in no.

- (1) Binary  $\rightarrow$  Base 2 (0, 1)
- (2) Octal  $\rightarrow$  Base 8 (0, 1, 2, 3, 4, 5, 6, 7)
- (3) Decimal  $\rightarrow$  Base 10 (0, 1, 2, 3, 4, 5, 6, 7, 8, 9)
- (4) Hexadecimal  $\rightarrow$  Base 16 (0, 1, 2, 3, 4, 5, 6, 7, 8, 9, A, B, C, D, E, F)

### Conversion

$\rightarrow$  Any no to decimal number system

ex:  $[101.010]_2$  to decimal

$$\begin{array}{r}
 1 \times 2^2 \\
 0 \times 2^1 \\
 1 \times 2^0
 \end{array}
 \left[ \begin{array}{c}
 \leftarrow 1 \\
 \leftarrow 0 \\
 \leftarrow 1
 \end{array} \right]
 \left[ \begin{array}{c}
 2 \\
 1 \\
 0
 \end{array} \right]
 \left[ \begin{array}{c}
 \leftarrow 0 \\
 \leftarrow 1 \\
 \leftarrow 0
 \end{array} \right]
 \left[ \begin{array}{c}
 2^{-1} \\
 2^{-2} \\
 2^{-3}
 \end{array} \right]$$

$$4 + 0 + 1 + 0 + 2^{-2} + 0 \\
 5 + \frac{1}{4} = (5.25)_{10}$$

$$\begin{array}{r}
 4 \times 5^3 \\
 0 \times 5^2 \\
 2 \times 5^1 \\
 1 \times 5^0
 \end{array}
 \left[ \begin{array}{c}
 \leftarrow 4 \\
 \leftarrow 0 \\
 \leftarrow 2 \\
 \leftarrow 1
 \end{array} \right]
 \left[ \begin{array}{c}
 3 \\
 2 \\
 1 \\
 0
 \end{array} \right]
 \left[ \begin{array}{c}
 \leftarrow 2 \\
 \leftarrow 1 \\
 \leftarrow 0
 \end{array} \right]
 \left[ \begin{array}{c}
 5^{-1} \\
 5^{-2} \\
 5^{-3}
 \end{array} \right]$$

$$= 5^3 + 0 + 10 + 1 + 0.4 \\
 = [511.4]_{10}$$



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Q [13]<sub>10</sub> to binary

2	13	1	↑	[1101] <sub>2</sub>
2	6	0		
2	3	1		
	1			

Q [13.31]

2	13	1	↑
2	6	0	
2	3	1	
	1		

$0.31 \times 2 = 0.62$	0	↓
$0.62 \times 2 = 1.24$	1	
$0.24 \times 2 = 0.48$	0	

So  $[13.31]_{10} \rightarrow [1101.010]_2$

Q [546.976]<sub>10</sub> → [ ]<sub>8</sub>

8	546	2	↑
8	68	4	
8	0	0	
	1		

$0.976 \times 8 = 7.808$	7	↓
$0.808 \times 8 = 6.464$	6	

So

$[1042.76]_8$



Q [336.234]<sub>10</sub> → [ ]<sub>16</sub>

$$\begin{array}{r|l} 16 & 336 \\ \hline & 21 \\ & 1 \end{array} \begin{array}{l} 0 \\ 5 \end{array}$$

$$0.234 \times 16 = 3.744 \quad 3$$

$$0.744 \times 16 = 11.904 \quad 11$$

$$0.904 \times 16 = 14.469 \quad 14$$

$$= (150.3BF)_{16}$$

→ Any base to any base

$$[Num]_b \rightarrow [decimal]_{10} \rightarrow [Num]_q$$

Q [111011] → [ ]<sub>8</sub>

$$2^5 + 2^4 + 2^3 + 2 + 1 = [59]_{10}$$

$$\begin{array}{r|l} 8 & 59 \\ \hline & 7 \end{array} \begin{array}{l} 3 \end{array}$$

$$[73]_8$$

Q [323]<sub>4</sub> → [ ]<sub>16</sub>

~~$$\begin{array}{r|l} 4 & 323 \\ \hline & 3 \\ & 2 \\ & 3 \end{array}$$~~

$$3 \times 4^2 + 2 \times 4 + 3$$

$$[59]_{10}$$

$$\begin{array}{r|l} 16 & 59 \\ \hline & 3 \end{array} \begin{array}{l} 11 \end{array}$$

$$\Rightarrow [3B]_{16}$$



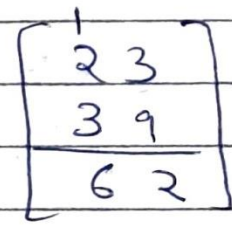
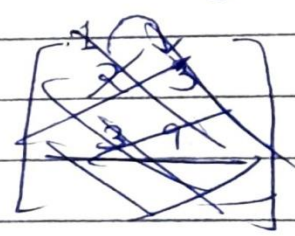
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Q Write Decimal no 0 to 15 in Binary

0	0000
1	0001
2	0010
3	0011
4	0100
5	0101
6	0110
7	0111
8	1000
9	1001
10	1010
11	1011
12	1100
13	1101
14	1110
15	1111

Binary Arithmetic

→ Addition:



Sum - Base  
 $12 - 10 = 2$



$$\begin{array}{r} 0 \\ + \begin{array}{|c|c|c|c|} \hline 1 & 1 & 0 & 1 \\ \hline 0 & 1 & 0 & 1 \\ \hline 1 & 0 & 0 & 1 & 0 \\ \hline \end{array} \\ \hline \end{array} \quad 2 \quad 2-2=0$$

$$\begin{array}{r} 0 \\ \begin{array}{|c|c|c|c|} \hline 1 & 0 & 1 & 0 \\ \hline 0 & 1 & 0 & 1 \\ \hline 1 & 1 & 1 & 1 \\ \hline 1 & 1 & 1 & 1 & 0 \\ \hline \end{array} \\ \hline \end{array} \quad 2 \quad \begin{array}{l} 2-2=0 \\ 3-2=1 \end{array}$$

Binary  
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$$\begin{array}{r} 0 \\ \begin{array}{|c|c|c|c|c|c|c|} \hline 0 & 1 & 1 & 0 & 1 & 0 & 1 & 0 \\ \hline 0 & 0 & 0 & 0 & 1 & 0 & 0 & 0 \\ \hline 1 & 0 & 0 & 0 & 0 & 0 & 0 & 1 \\ \hline 1 & 1 & 1 & 1 & 1 & 1 & 1 & 1 \\ \hline 1 & 1 & 1 & 1 & 1 & 0 & 0 & 1 & 0 \\ \hline \end{array} \\ \hline \end{array} \quad 2$$

Note  
 If no of 1's in a column even then sum = 0  
 If no of 1's in a column odd then sum = 1  
 each pair gives carry to the next line

Subtraction:

$$\begin{array}{r} 6 \quad 10+2 \\ \begin{array}{|c|c|} \hline 7 & 2 \\ \hline 1 & 5 \\ \hline 5 & 7 \\ \hline \end{array} \\ \hline \end{array} \quad 10$$



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$$\begin{array}{r} \textcircled{0} \\ \begin{array}{r} \textcircled{1} \downarrow \textcircled{2} \\ \begin{array}{r} 10 + 0 \\ \hline 0111 \\ \hline 0011 \end{array} \end{array} \end{array} \textcircled{2}$$

### Complements

Complement simplify subtraction because it perform subtraction with the help of addition

Complements are 2 types

- ①  $n$ 's complement-
- ②  $(n-1)$ 's complement-

→  $n$ 's complement-:

eg  $[N]_n$  then  $n$ 's complement is

$$= \begin{cases} n^n - N & \text{if } N \neq 0 \\ 0 & \text{if } N = 0 \end{cases}$$

where  $n$  is the number of digits in integer part

①  $[10110]_2$   $2$ 's complement is :-

$$\begin{array}{r} 2^5 - 10110 \\ 32 - 10110 \\ \hline 10000 - 10110 \\ 2's \text{ complement} = 1010 \end{array}$$

$$\begin{array}{r|l} 2 & 32 \\ \hline & 16 \\ \hline 2 & 8 \\ \hline 2 & 4 \\ \hline 2 & 2 \\ \hline & 1 \end{array}$$





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→  $(r-1)$ 's Complement

$$(r-1)'s \text{ Complement} = \begin{cases} r^n - r^{-m} - N & N \neq 0 \\ 0 & N = 0 \end{cases}$$

where  $n$  is the number of digits in integer part  
 $m$  is the number of digits in fractional part

①  $[101100]_2$  1's complement

$$2^6 - 1 - 101100$$

$$63 - 101100 = 101111 - 101100$$

$$[010011]$$

Subtraction using 2's Complement

①  $[110010]_2 - [100000]_2$

Step 1:  $m = 110010$

$$N = 100000$$

$$\text{Balance: } N = 010000$$

Step 2: Take 2's complement of N

$$N' = \cancel{100000} 110000$$

Step 3:  $m + N'$

$$110010 + 110000$$

$$\textcircled{1} 000010$$

discard  $\Rightarrow 100010$  Ans



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$$\textcircled{1} [10000]_2 - [110010]_2$$

$$M = 010000$$

$$N = 110010$$

$$N' = 001110$$

$$M + N'$$

$$010000 + 001110$$

$$011110$$

Carry not generated So number is -ve

Now taking 2's complement of result.

$$= -100010$$

$$\textcircled{2} 1010 - 1011$$

$$= 0011$$

$$\textcircled{3} 11111 - 101100$$

$$= 10011$$

$$\textcircled{4} 101100 - 11111$$

$$= -10011$$

Subtraction using 1's complement

$$\textcircled{1} [110010]_2 - [10000]_2$$

$$M = 110010$$

$$N = 010000$$



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Take 1's complement of N.

$$N' = 10111$$

$$M + N' = 110010 + 10111$$

$$= \textcircled{1}10001$$

$$+ \quad \xrightarrow{\quad} \quad \underline{\quad}$$

$$100010 \quad \text{Ans}$$

$$\textcircled{1} \quad [10000]_2 - [110010]$$

$$M = 010000$$

$$N = 110010$$

$$N' = 001101$$

$$M + N' = 010000 + \textcircled{0}01101$$

$$= 011101$$

Carry not generate so take 1's complement of result

$$= -100010 \quad \text{Ans}$$

and number is -2

$$\textcircled{1} \quad 101100 - 111111$$

$$\textcircled{1} \quad 1111 - 1010$$



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## Boolean Algebra

Binary variable can be represented by X, Y, A, B... etc.

All binary variable can have 2 values i.e. 0 and 1

### Rules for minimizing Boolean functions:

- |  |   |
|--|---|
| ① $A + 0 = A$                            | ⑪ $A \cdot 1 = A$   |
| ② $A + 1 = 1$                            | ⑫ $A \cdot 0 = 0$   |
| ③ $A + A = A$                            | ⑬ $A \cdot A = A$   |
| ④ $A + \bar{A} = 1$                      | ⑭ $A \cdot \bar{A} = 0$                                     |
| ⑤ $A \cdot (B + C) = AB + AC$            | ⑮ $A + BC = (A + B)(A + C)$                                 |
| ⑥ $A + AB = A$                           | ⑯ $A(A + B) = A$  |
| ⑦ $A + \bar{A}B = A + B$                 | ⑰ $A(\bar{A} + B) = AB$                                     |
| ⑧ $AB + A\bar{B} = A$                    | ⑱ $(A + B)(A + \bar{B}) = A$                                |
| ⑨ $AB + \bar{A}C = (A + C)(B + \bar{A})$ | ⑲ $(A + B)(\bar{A} + C) = AC + \bar{A}B$                    |
| ⑩ $AB + \bar{A}C + BC = AB + \bar{A}C$   | ⑳ $(A + B)(\bar{A} + C)(B + C)$<br>$= (A + B)(\bar{A} + C)$ |

① minimize :-  $(A + B + C)(A + B + \bar{C})(A + \bar{B} + C)$

$(\cancel{A\bar{A}} + \overset{A}{A}B + \overset{A}{A}\bar{C} + \bar{B}A + \bar{B}\bar{B} + \bar{B}C + \bar{A}C + \bar{C}(B + \bar{C})) (A + \bar{B} + C)$

$(A + \bar{A}\bar{B} + \bar{A}\bar{C} + \bar{B}\bar{C} + AC + \bar{C}B) (A + \bar{B} + C)$

$(A + \bar{B} + \bar{A}) (A + \bar{B} + C)$

$(A + \bar{B}) (A + \bar{B} + C)$

$A + \bar{A}\bar{B} + AC + \bar{A}B + \bar{B}C$

$A + A + \bar{B}C$

$(A + \bar{B}C)$

Ans



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Q) Minimize:  $AB\bar{C}\bar{D} + AB\bar{C}D + A\bar{B}\bar{C}D + ABCD + ABC\bar{D} + A\bar{B}C\bar{D}$

$$AB\bar{C}\bar{D} + AC\bar{D} + AB\bar{C} + A\bar{B}C$$

$$AB\bar{C}\bar{D} + A\bar{C}D + AC$$

$$A\bar{C}(B\bar{D} + D) + AC$$

$$A\bar{C}(B+D) + AC$$

$$A\bar{C}B + A\bar{C}D + AC$$

$$A\bar{C}(\bar{B} + C) + A\bar{C}D$$

$$A(B+C) + A\bar{C}D$$

$$AB + AC + A\bar{C}D$$

$$AB + A(C + \bar{C}D)$$

$$AB + AC(C+D)$$

$$AB + AC + AD$$

Ans

Q) Minimize:  $\bar{P}(P+QR) + (P\bar{Q} + \bar{Q}R)$

$$\bar{P}QR + P\bar{Q} + \bar{Q}R$$

$$R(\bar{P}\bar{Q} + \bar{Q}) + P\bar{Q}$$

$$R(\bar{P} + \bar{Q}) + P\bar{Q}$$

$$R\bar{P} + R\bar{Q} + P\bar{Q}$$

Ans

Q) Minimize:  $\bar{A}(\bar{M} + \bar{A})(M + \bar{M} + A)$

$$\bar{A}\bar{M}(M+A) \quad (\bar{A}\bar{M} + \bar{A})(M+A)$$

$$\bar{A}\bar{M}M + \bar{A}\bar{M}A$$

$$\bar{A}\bar{M} + \bar{A}\bar{M}A$$

$$= \bar{A}\bar{M}$$



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① Minimize:  $F \bar{T} + \bar{F} + \bar{T} \bar{F}$   
 $\bar{F} + \bar{F}$  Ans

② Simplify:  $AV(A+\bar{V}) + A(\bar{V}+\bar{V})$   
 $AV + A$   
 $A$  AS

③ For  $F = (J + K\bar{L})(JK + L)$   
 $JK + JK$   
 $J(K + L)$  AS

De-Morgan Law

$\overline{A \cdot B \cdot C \cdot D \dots} \Rightarrow \bar{A} + \bar{B} + \bar{C} + \bar{D} + \dots$

$\overline{A + B + C + D \dots} \Rightarrow \bar{A} \bar{B} \bar{C} \bar{D} \dots$

④ Reduce:  $F = (x\bar{y}) + (\bar{x}y)$   
 $= (\overline{x\bar{y}})(\overline{\bar{x}y})$   
 $= (\bar{x} + y)(\bar{x} + \bar{y})$  Ans

⑤  $y = (a + \bar{b} + c + \bar{a}) + (b + \bar{c})$   
 $= (\overline{a + \bar{b} + c + \bar{a}})(\overline{b + \bar{c}})$   
 $= (\bar{a} \bar{b} \bar{c} \bar{d})(\bar{b} \bar{c})$   
 $= \bar{a} \bar{b} \bar{c} \bar{c} \bar{d} = 0$



Conical / standard form

Sum of product (SOP)

Ex

$$xy + yz + zx$$

→ Under SOP each product term called minterms

→ Each minterms are not contain all variable than it is called standard form

→ If each minterm contain all variable than it is called conical form

→ Convert - std to conical

$$xy + yz + zx$$

$$xy(z + \bar{z}) + yz(x + \bar{x}) + zx(y + \bar{y})$$

$$xyz + xy\bar{z} + x\bar{y}z + x\bar{y}\bar{z} + \bar{x}yz + \bar{x}y\bar{z} + x\bar{y}z + x\bar{y}\bar{z}$$

$$\begin{matrix} xyz + xy\bar{z} + \bar{x}y\bar{z} + x\bar{y}\bar{z} \\ 111 \quad 110 \quad 011 \quad 101 \end{matrix}$$

$$\sum_{min} (3, 5, 6, 7)$$

Product of sum (POS)

$$(\bar{x} + y)(x + \bar{y})(\bar{z} + x)$$

→ Under POS each sum term is called max term

→ Each max term are not contain all variable than it is called standard form

→ If each max term contain all variable than it is called conical form

$$(x + y)(\bar{x} + \bar{y})(\bar{z} + x)$$

$$(\bar{x} + y + z\bar{z})(x + \bar{y} + z\bar{z})$$

$$(\bar{z} + x + y\bar{y})$$

$$(\bar{x} + y + z)(\bar{x} + y + \bar{z})(x + \bar{y} + z)$$

$$(\bar{x} + \bar{y} + \bar{z})(x + y + z)(x + \bar{y} + \bar{z})$$

$$\Rightarrow (\bar{x} + y + z)(\bar{x} + y + \bar{z})(x + \bar{y} + z)$$

$$100 \quad 100 \quad 010$$

$$(\bar{x} + \bar{y} + \bar{z})(x + y + z)$$

$$011 \quad 000$$

$$\prod_m (0, 2, 3, 4, 5)$$



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Q) Convert SOP to POS

~~f(A)~~  $F = A + \bar{B}C$

Sol  $= A(B + \bar{B})(C + \bar{C}) + (A + \bar{A})\bar{B}C$   
 $= (AB + A\bar{B})(C + \bar{C}) + A\bar{B}C + \bar{A}\bar{B}C$   
 $= ABC + AB\bar{C} + \underline{A\bar{B}C} + \underline{A\bar{B}\bar{C}} + \underline{A\bar{B}C} + \bar{A}\bar{B}C$   
 $= ABC + AB\bar{C} + A\bar{B}C + \bar{A}\bar{B}C + A\bar{B}C$   
 111 110 100 001 101

$\sum_m (1, 4, 5, 6, 7)$

$\prod_m (0, 2, 3)$

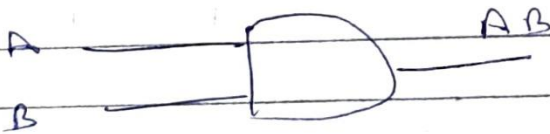
$(A + B + C)(A + \bar{B} + C)(A + \bar{B} + \bar{C})$

Logic Gates

Basic Gates :-

①

AND Gate



A	B	Y
0	0	0
0	1	0
1	0	0
1	1	1

②

OR Gate



A	B	Y
0	0	0
0	1	1
1	0	1
1	1	1





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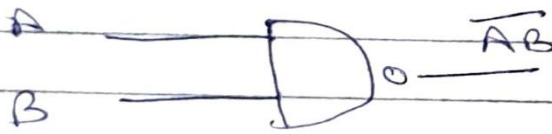
③ Not Gate :-



A	Y
0	1
1	0

Universal Gates

① NAND Gate :-



A	B	Y
0	0	1
0	1	1
1	0	1
1	1	0

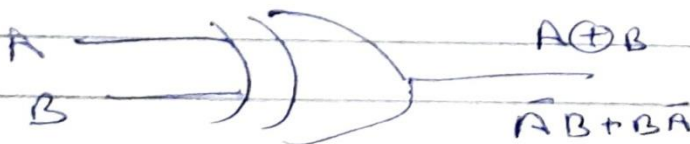
② NOR Gate :-



A	B	Y
0	0	1
0	1	0
1	0	0
1	1	0

Special purposes Gate :-

① Ex OR

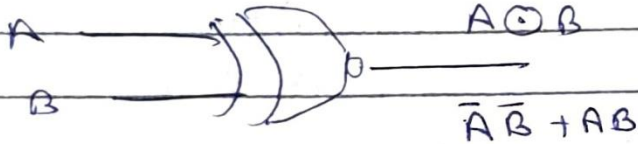


A	B	Y
0	0	0
0	1	1
1	0	1
1	1	0



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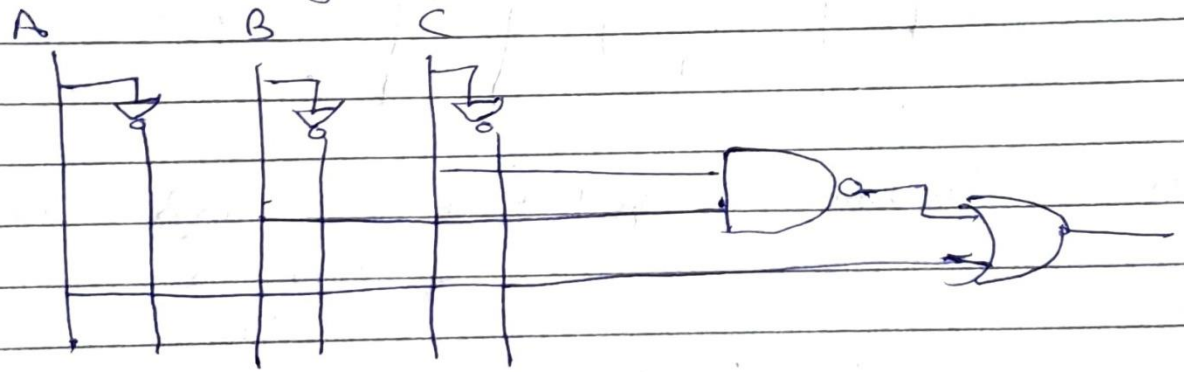
② Ex NOR



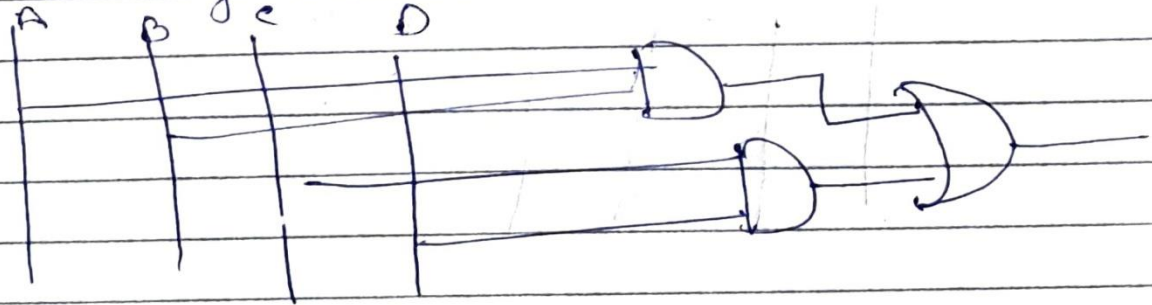
A	B	Y
0	0	1
0	1	0
1	0	0
1	1	1

③ Implement using Basic Gate

$A + \bar{B}C$



④ Implement using Basic Gate:  $AB + CD$

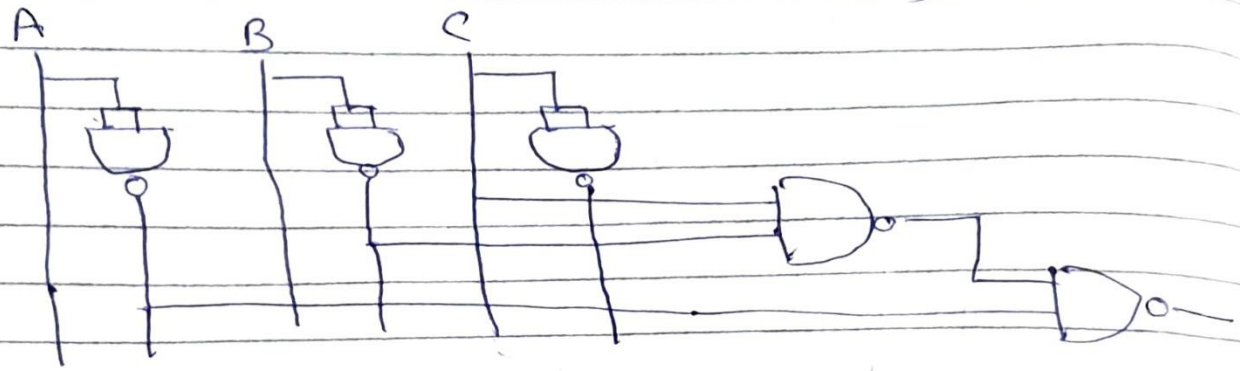




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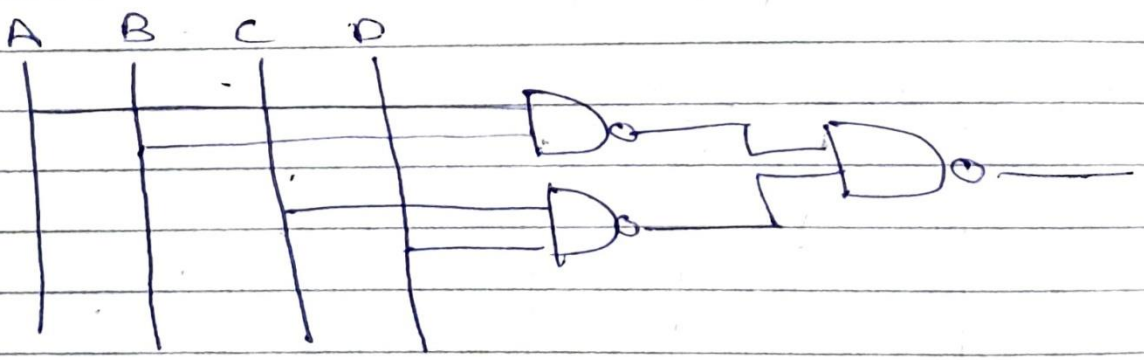
Q Implement using NAND Gate:  $A + \bar{B}C$

$$\overline{\overline{A + \bar{B}C}}$$

$$\overline{\bar{A}(\bar{B}C)}$$


Q Implement using NAND Gate:  $AB + CD$

$$\overline{\overline{AB + CD}}$$

$$\overline{\bar{A}\bar{B}\bar{C}\bar{D}}$$


Q Implement using NOR Gate  $A + \bar{B}C$

$$\overline{\overline{A + \bar{B}C}}$$

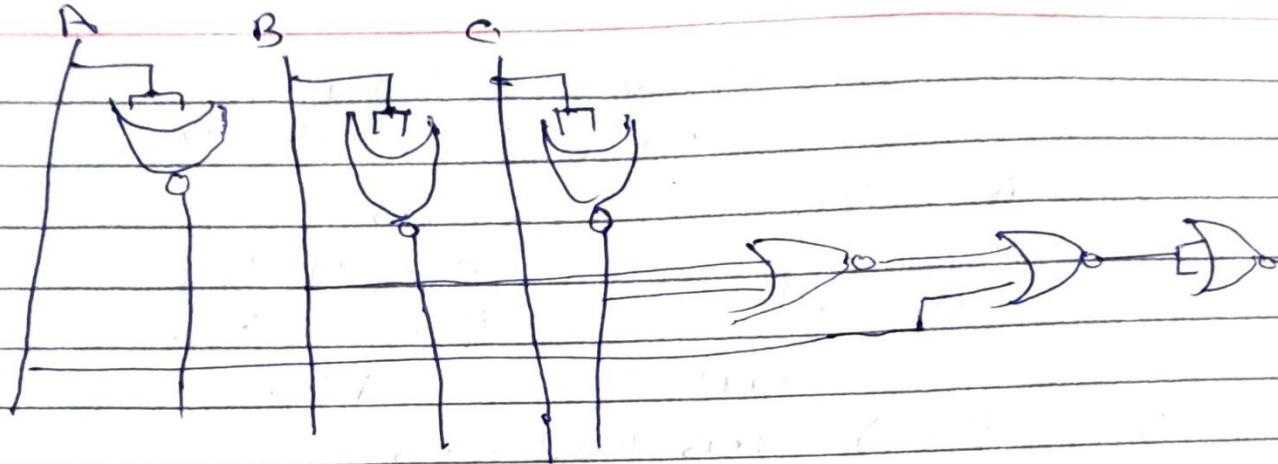
$$\overline{\bar{A}(\bar{B}C)}$$

$$\overline{\bar{A}(B + \bar{C})}$$

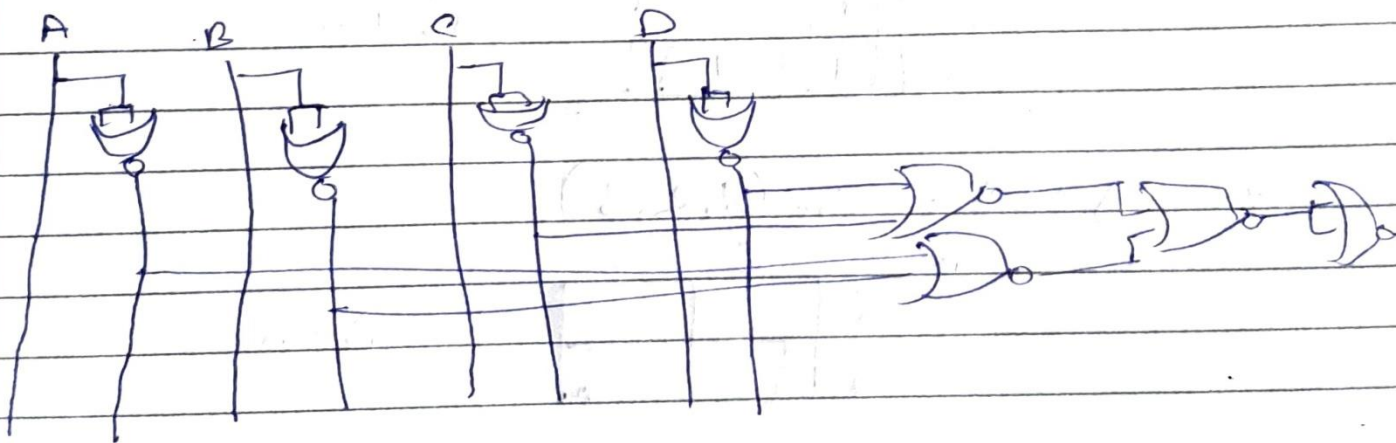
$$A + \bar{B} + \bar{C}$$



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Implement using NOR Gate  $AB + CD$   
 $\overline{\overline{A + B} + \overline{C + D}}$



### K map

Boolean algebra deals with 0 and 1 but not X (don't care) condition. K-map deals with don't care 0 and 1

K map gives minimized solution

K-map does not give unique solution

No. of cells in any K map =  $2^n$  ( $n = \text{no. of variables}$ )



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2 variable kmap

no. of cells =  $2^2 = 4$

	B	$\bar{B}$
A	0	1
$\bar{A}$	2	3

SOP

	B	$\bar{B}$
A	0	1
$\bar{A}$	2	3

POS

①  $f(A,B) = \bar{A}\bar{B} + AB + A\bar{B}$

$\sum_m (0, 2, 3)$

	B	$\bar{B}$
A	1	
$\bar{A}$	1	1

$\bar{B} + A$

②  $f(A,B) = \sum_m (1, 2, 3)$

	B	$\bar{B}$
A		1
$\bar{A}$	1	1

$B + A$

③  $f(A,B) = (\bar{A} + \bar{B})(A + B)(A + \bar{B}) \Rightarrow \prod_m (0, 1, 3)$

	B	$\bar{B}$
A	0	0
$\bar{A}$		0

$A\bar{B}$

④  $\prod_m (1, 2, 3)$

	B	$\bar{B}$
A		0
$\bar{A}$	0	0

$\bar{A}\bar{B}$



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3 variable kmap

No. of cell =  $2^3 = 8$

		$B^c$			
		$\bar{B}^c$	$B^c$	$B^c$	$\bar{B}^c$
$A$	$\bar{A}$	0	1	3	2
	$A$	4	5	7	6

SOP

		$B^c$			
		$B^c$	$\bar{B}^c$	$\bar{B}^c$	$B^c$
$A$	$A$	0	1	3	2
	$\bar{A}$	4	5	7	6

POS

- Q Minimize  $ab + \bar{B}c + bc$   
 $ab(c + \bar{c}) + (a + \bar{a})\bar{B}c + (a + \bar{a})bc$   
 $abc + ab\bar{c} + a\bar{B}c + \bar{a}Bc + abc + a\bar{B}c$   
 $abc + ab\bar{c} + a\bar{B}c + \bar{a}Bc + \bar{a}Bc$   
 $\sum_m (1, 3, 5, 6, 7)$

		$bc$			
		$\bar{b}^c$	$\bar{b}^c$	$b^c$	$b^c$
$a$	$\bar{a}$		1	1	
	$a$		1		1

$c + ab$

- Q  $\sum_m (0, 1, 4, 5, 6)$

		$B^c$			
		$\bar{B}^c$	$\bar{B}^c$	$B^c$	$B^c$
$A$	$\bar{A}$	1	1		
	$A$	1	1		1

$\bar{b} + a\bar{c}$

- Q Draw Kmap of  $A \odot B \odot C$  or  $A \oplus B \oplus C$

		$B^c$			
		$\bar{B}^c$	$\bar{B}^c$	$B^c$	$B^c$
$A$	$\bar{A}$		1		1
	$A$	1		1	0



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4 variable K map

No of cells =  $2^4 = 16$

AB \ CD	$\bar{C}\bar{D}$	$\bar{C}D$	$CD$	$C\bar{D}$
$\bar{A}\bar{B}$	0	1	3	2
$\bar{A}B$	4	5	7	6
$AB$	12	13	15	14
$A\bar{B}$	8	9	11	10

AB \ CD	$\bar{C}\bar{D}$	$\bar{C}D$	$CD$	$C\bar{D}$
$A\bar{B}$	0	1	3	2
$A+B$	4	5	7	6
$\bar{A}+B$	12	13	15	14
$\bar{A}+B$	8	9	11	10

SOP

Q

$\Sigma m(1, 2, 4, 5, 6, 7, 8, 9, 10, 11)$

AB \ CD	$\bar{C}\bar{D}$	$\bar{C}D$	$CD$	$C\bar{D}$
$\bar{A}\bar{B}$		1		1
$\bar{A}B$	1	1	1	1
$AB$				
$A\bar{B}$	1	1	1	1

$\bar{A}\bar{B} + A\bar{B} + \bar{A}\bar{C}D + \bar{A}C\bar{D}$

Q

$\Sigma m(0, 1, 2, 3, 8, 9, 10, 11)$

AB \ CD	$\bar{C}\bar{D}$	$\bar{C}D$	$CD$	$C\bar{D}$
$\bar{A}\bar{B}$	1	1	1	1
$\bar{A}B$				
$AB$				
$A\bar{B}$	1	1	1	1

$\bar{B}$



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Q  $\Sigma_m(0, 1, 5, 7, 8, 10, 14, 15)$

	$\bar{C}\bar{D}$	$\bar{C}D$	$CD$	$C\bar{D}$
$\bar{A}\bar{B}$	1	1		
$\bar{A}B$		1	1	
$AB$			1	1
$A\bar{B}$	1			1

Ans  $\bar{B}\bar{C}D + \bar{A}\bar{C}D + B\bar{C}D + A\bar{C}\bar{D}$

Ans  $\bar{A}\bar{B}\bar{C} + \bar{A}B\bar{D} + A\bar{B}C + A\bar{B}\bar{D}$

5 variable Kmap

No of cells =  $2^5 = 32$

→ 16  
→ 16

	$\bar{A}$			
$\bar{B}\bar{C}$	$\bar{D}\bar{E}$	$\bar{D}E$	$DE$	$D\bar{E}$
$\bar{B}C$	0	1	3	2
$B\bar{C}$	4	5	7	6
$BC$	12	13	15	11
$B\bar{C}$	8	9	11	10

	$A$			
$\bar{B}\bar{C}$	$\bar{D}\bar{E}$	$\bar{D}E$	$DE$	$D\bar{E}$
$\bar{B}C$	16	17	19	18
$B\bar{C}$	20	21	23	22
$BC$	28	29	31	30
$B\bar{C}$	24	25	27	26

Q  $\Sigma(0, 1, 6, 13, 14, 15, 16, 17, 22, 25, 27, 30)$





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		$\bar{A}$				$A$			
		$\bar{D}\bar{E}$	$\bar{D}E$	$D\bar{E}$	$DE$	$\bar{D}\bar{E}$	$\bar{D}E$	$D\bar{E}$	$DE$
$\bar{B}$	$\bar{C}$	1	1			1	1		
	$C$				1				1
	$\bar{C}$			1	1				1
	$C$							1	1

$$\bar{D}\bar{B}\bar{C} + D\bar{E}C + B\bar{C}E\bar{A} + B\bar{C}EA$$

Don't care condition

Don't care means uncertain value it may be 0 and 1

①  $\Sigma_m(0, 1, 2, 8, 9) + d(4, 10, 12)$

$\bar{A}B$		$\bar{C}$				$C$			
		$\bar{D}\bar{E}$	$\bar{D}E$	$D\bar{E}$	$DE$	$\bar{D}\bar{E}$	$\bar{D}E$	$D\bar{E}$	$DE$
$\bar{A}$	$\bar{B}$	1	1			1			
	$B$	x							
	$\bar{A}$								
	$A$	1	1			x			

$$B\bar{C} + \bar{B}\bar{D}$$

0-63

$2^6 = 64$

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6 variable Kmap

Q)  $\Sigma m(2, 3, 6, 7, 8, 12, 14, 17, 19, 21, 23, 25, 27, 28, 29, 30, 32, 33, 34, 35, 40, 44, 46, 49, 51, 53, 55, 57, 59, 61, 62, 63)$

$\bar{A}\bar{B}$

EF	$\bar{E}\bar{F}$	$\bar{E}F$	$E\bar{F}$	$EF$
$\bar{C}\bar{D}$	0	1	2	3
$\bar{C}D$	4	5	6	7
$C\bar{D}$	8	9	10	11
$CD$	12	13	14	15

$\bar{A}B$

EF	16	17	18	19
$\bar{C}\bar{D}$	20	21	22	23
$\bar{C}D$	24	25	26	27
$C\bar{D}$	28	29	30	31
$CD$	32	33	34	35

$A\bar{B}$

EF	36	37	38	39
$\bar{C}\bar{D}$	40	41	42	43
$\bar{C}D$	44	45	46	47
$C\bar{D}$	48	49	50	51
$CD$	52	53	54	55

$AB$

EF	56	57	58	59
$\bar{C}\bar{D}$	60	61	62	63
$\bar{C}D$	64	65	66	67
$C\bar{D}$	68	69	70	71
$CD$	72	73	74	75

$\bar{A}\bar{B}\bar{C}\bar{E} + \bar{A}\bar{B}\bar{C}F + \bar{A}\bar{B}\bar{E}F + \bar{A}\bar{B}C\bar{D}\bar{E} + \bar{A}\bar{B}C\bar{D}F$   
 $+ \bar{A}\bar{B}C\bar{D} + \bar{A}B\bar{C}D + \bar{A}B\bar{C}E\bar{F} + \bar{A}B\bar{C}EF$   
 $+ \bar{A}B\bar{C}\bar{E}F + \bar{A}B\bar{C}EF$

